

$\hat{p} = 32\%$
Population
Focus Proportion

$\rho_0 = 35\%$ $\alpha = 5\%$
Voters in the United States
Adults Who Supported Romney

$n = 450$

Step I Identify Procedure:

We want to test the evidence against the claim that the proportion of **adults who supported Romney** in the population of **voters in the United States** (ρ) is equal to **35%** (ρ_0).

The null and alternative hypotheses are:

$$H_0: \rho = 35\%$$

$$H_A: \rho < 35\%$$

Step II Check Conditions:

* **Random Sample:** A **random sample** was conducted to insure every member of the population was equally likely to be selected.

* **Normal Sampling Distribution:** The sampling distribution of all possible sample proportions has an approximately **normal** shape because:

$$n * \rho > 10$$
$$450 * 35\% > 10$$

$$n * (1 - \rho) > 10$$
$$450 * (1 - 35\%) > 10$$

* **Independence:** The lack of replacement is not a problem in this case because the number of subjects in the population is more than **10** times the sample size.

Step III Perform Procedure:

See "Graph B4" tab for graph of sampling distribution

Sampling Distribution: Proportion = **35%** Standard Deviation = $\frac{\sqrt{\rho(1-\rho)}}{\sqrt{n}} = \frac{(35\%(1-35\%)^{0.5})}{\sqrt{450}} = \mathbf{2.2\%}$
 Shape: Approximately **Normal**

P-Value = $P(\hat{p} < 32\% \mid \rho = 35\%) = \mathbf{8.6\%}$ compared to the Significance Level (α) of **5%**

Step IV Interpretation:

We fail to reject the null hypothesis at the **5%** significance level (α). The P-value of **8.6%** shows that an observed sample proportion as extreme as **32%** (\hat{p}) would be expected to occur **8.6%** of the time, and thus mere chance could explain the difference between the sample proportion and hypothesized population proportion. We cannot say that the proportion of **adults who supported Romney** in the population of **voters in the United States** is not equal to the reported proportion of **35%** (ρ_0).